

## Basic Types of Quantitative Comparisons

## SOLUTIONS

1. Identify the type of quantitative comparison in the given statements.
a. Value
b. Absolute difference
c. Ratio (relative difference)
d. Percentage change
e. Absolute difference
f. Ratio (relative difference)
g. Rank (median is the 50th percentile)
h. $Z$-score (standardized value)
i. Value (in this case, the units of measurement are percentage points)
j. Rank
2. Identify the correct statements; rewrite the incorrect statements to correct them.
a. "Brand X lasts longer than Brand T, with an average lifetime $40 \%$ higher than Brand T's."
b. Correct as written.
c. "The ratio of flour to butter in shortbread is 2:1; the recipe uses twice as much flour as butter."
d. Correct as written.
e. "Nadia's test score was higher than $84 \%$ of students nationwide ( $Z=$ 1.0)." (Sixty-six percent are within 1 standard deviation of the mean [e.g., $\pm 1$ standard deviation], but you must also include those for which $z<-1.0$ to answer this question correctly.)
f. "A panel of 200 consumers rated ISP A four to one over ISP B. In other words, four times as many panelists preferred Company A as their Internet service provider."
g. Correct as written.
h. Correct as written.
i. "The value of mutual fund ABCD tripled since last year, going from 33 to 100."
3. Fill in the missing information.
a. "Asians make about twice as much income as blacks."
b. "Hispanics earn $\$ 2,825$ more than blacks."
c. "Whites rank second in terms of median income, below only Asians and Pacific Islanders."
d. "Asians earn $20 \%$ more than whites."
4. With a comparison value of $\$ 200$ :

The two phrases " $25 \%$ of the original price" (item a) and "marked down $75 \%$ " (f) have the same meaning. Each of those phrases corresponds to a price of $\$ 50$, equivalent to a ratio of 0.25 .
The phrases "costs $25 \%$ less than . . " (item b), "priced $25 \%$ off" (d), " $75 \%$ of the original price" (g), and "costs $75 \%$ as much as . . ." (h) are equivalent. They correspond to a price of $\$ 150$, equivalent to a ratio of 0.75 .
The two phrases "costs $25 \%$ more than . . ." (item c) and " $125 \%$ of the original price" (e) have the same meaning. They correspond to a price of $\$ 250$ and a ratio of 1.25 .
9. Fill in the $z$-score for height for each boy in the sample.

Table 8C. Heights of a sample of six-year-old boys
(standard population: mean $=\mathbf{1 1 5 . 1 2} \mathbf{~ c m} ; S D=4.78 \mathbf{c m}$ )

| Name | Height (cm) | Z-score |
| :--- | :--- | ---: |
| David | 117.51 | 0.50 |
| Jamal | 113.90 | -0.26 |
| Ryan | 124.81 | 2.03 |
| Luis | 115.45 | 0.07 |
| JC | 112.73 | -0.50 |

SD = standard deviation
a. Ryan is approximately two standard deviations above the average height for a six-year-old boy, while Luis is just about average and JC is half a standard deviation below average for his age.
b. David and JC are half a standard deviation taller and shorter than the average six-year-old boy, respectively.
c. Mike stands 119.90 cm tall.
11. Answer the questions about attributable risk from the information given.
a. The attributable risk of hospital admission associated with diabetes is calculated: $[0.05(3.5-1)] /[(0.05[3.5-1])+1] \times 100=11.1 \%$. Prevalence is expressed as a proportion in the calculation.
b. If diabetes could be eliminated, hospital admissions would decline by $11 \%$.

